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# Improved $(g-2)_{\mu}$ measurements and SUSY

02/03/2021 BASED ON : 2006.15157, EPJC WITH SVEN HEINEMEYER AND IPSITA SAHA

- EW sector may be hiding key to new physics
- Modest production cross section, mass bounds from the LHC comparably weak
- May show up elsewhere : DM experiments,  $(g-2)_{\mu}$  ....

 New results from Fermilab 'MUON (g-2)' coming soon !



# Outline

- Status of  $(g 2)_{\mu}$
- EW sector of MSSM
- Experimental constraints
- Results
- Future collider prospects
- Conclusion



 $-\sigma^{\mu\nu}q_{\nu}F_{2}($  $\mu(p)A_{\mu}$  $\bar{u}(p')[\gamma^{\mu}F_1(q^2)$  $2m_{\mu}$ 

 $F_2(0) = a_{\mu}$ 



# <u>Muon (g-2)</u>



Keshavarzi, Nomura, Teubner '20



# MSSM particle content



# Standard particles

# **SUSY** particles



Masses and mixing are determined by U(1) and SU(2) gaugino masses  $M_1$ ,  $M_2$  and Higgs mass parameter  $\mu$ .





Masses and mixing are determined by U(1) and SU(2) gaugino masses  $M_1, M_2$  and Higgs mass parameter  $\mu$ .

 $\tilde{W}^{3} = \begin{array}{c} M_{1} & 0 & -M_{Z} c_{\beta} s_{W} & M_{Z} s_{\beta} s_{W} \\ M_{u}^{0} & M_{N} = \begin{pmatrix} M_{1} & 0 & -M_{Z} c_{\beta} s_{W} & M_{Z} s_{\beta} s_{W} \\ 0 & M_{2} & M_{Z} c_{\beta} cW & -M_{Z} s_{\beta} cW \\ -M_{Z} c_{\beta} s_{W} & M_{Z} c_{\beta} c_{W} & 0 & -\mu \\ M_{Z} s_{\beta} s_{W} & -M_{Z} s_{\beta} c_{W} & -\mu & 0 \end{pmatrix}$ 

$$M_{C} = \begin{pmatrix} M_{2} & \sqrt{2}M_{W}c_{\beta} \\ \sqrt{2}M_{W}s_{\beta} & \mu \end{pmatrix}$$



Slepton Mass Matrix

$$M_{\tilde{L}}^{2} = \begin{pmatrix} m_{l}^{2} + m_{LL}^{2} & m_{l}X_{l} \\ m_{l}X_{l} & m_{l}^{2} + m_{RR}^{2} \end{pmatrix}$$

# PARAMETERS

First two gens.  $m_{\tilde{l}_1} \sim m_{LL}$   $m_{\tilde{l}_2} \sim m_{RR}$ 

$$m_{LL}^{2} = m_{\tilde{L}}^{2} + (I_{l}^{3L} - Q_{l}s_{w}^{2})M_{z}^{2}c_{2\beta}$$
$$m_{RR}^{2} = m_{\tilde{R}}^{2} + Q_{l}s_{w}^{2}M_{z}^{2}c_{2\beta}$$
$$X_{l} = A_{l} - \mu(\tan\beta)^{2I_{l}^{3L}}$$

# $M_1, M_2, \mu, \tan\beta, m_{\tilde{L}}, m_{\tilde{R}}$

# Constraints

Direct Searches at LHC

- LHC searches restricted to **simplified models**.
- $\tilde{\chi}_1^{\pm}$  and  $\tilde{\chi}_2^0$  taken to be mass-degenerate and purely wino.  $\tilde{\chi}_1^0$  purely bino.
- All three generations of sleptons and sneutrinos assumed mass degenerate. In MSSM:  $m_{\tilde{\nu}}^2 = m_{\tilde{l}}^2 + \frac{1}{2}m_Z^2\cos 2\beta$
- Heavier gauginos  $\tilde{\chi}_{3}^{0}$ ,  $\tilde{\chi}_{4}^{0}$ ,  $\tilde{\chi}_{2}^{\pm}$  assumed to be decoupled.
- No sensitivity to parameters like  $\tan \beta$ .

# **Proper recasting is important**

Indirect Constraints

- Muon (g-2).
- WMAP/PLANCK relic density.
- Spin independent direct detection data from XENON/LUX.
- Indirect detection constraints of dark matter.





SUSY contributions from Chargino-Sneutrino and Smuon-Neutralino loop

• SM EW 1 loop : 
$$\frac{\alpha}{\pi} \frac{m_{\mu}^2}{M_W^2}$$
.

• SUSY can easily explain anomaly !

upper limits on EW super partner masses



MSSM , 1 loop : 
$$\frac{\alpha}{\pi} \frac{m_{\mu}^2}{M_{SUSY}^2} \times tan\beta$$

# **SUSY contributions to** $(g-2)_{\mu}$

$$\Delta a_{\mu}(\tilde{W}, \tilde{H}, \tilde{\mu}_L) \simeq -2.5$$

$$\Delta a_{\mu}(\tilde{B}, \tilde{H}, \tilde{\mu}_R) \simeq -1.5$$



Endo, Hamaguchi, Iwamoto, Yoshinaga'13

# **A** Constraints



A well-tempered bino-wino or bino-higgsino LSP — Chargino coannihilation Bino - dominated LSP — Slepton coannihilation





# Searches at the LHC

• <u>Trilepton searches</u>

ATLAS [1803.02762] 13 TeV, 36 *fb*<sup>-1</sup>

- Pure wino-bino scenario
- 100% BR

• 
$$m_{\tilde{l}_L} = \frac{1}{2}(m_{\tilde{\chi}_1^{\pm}} + m_{\tilde{\chi}_1^0})$$

• 
$$m_{\tilde{l}_L} = m_{\tilde{\nu}}$$

•  $(\tilde{e}, \tilde{\mu}, \tilde{\tau})_L$  degenerate



Proper recasting is important **—>** checkMATE

# Searches at the LHC

• <u>Dilepton searches</u>

ATLAS [1908.08215] 13 TeV, 139  $fb^{-1}$ 





# LHC searches

• <u>Compressed spectra searches</u>

Soft leptons : ISR jet required to give boost



## ATLAS 1911.12606

# Searches at the LHC

• <u>Slepton pair production</u>

ATLAS [1908.08215]

13 TeV, 139  $fb^{-1}$ 





ATLAS 1911.12606

Proper recasting is important **—>** checkMATE



# Overview of CM



FIG. 1: Flow chart to demonstrate the chain of data processing within CheckMATE.

Drees, Dreiner, Schmeier, Tattersall, Kim '13 Kim, Schmeier, Tattersall, Rolbiecki '15 Dercks, Desai, Kim, Rolbiecki, Tattersall '16

# 

# Model testing

- Testing models against LHC analyses
- Signal events calculated for each SR

Evaluation of 
$$r = \frac{S - 1.96 \times \Delta S}{S_{exp}^{95}}$$

• For the best SR,  $r > 1 \longrightarrow \text{excluded}!$ 







Drees, Dreiner, Schmeier, Tattersall, Kim '13 Kim, Schmeier, Tattersall, Rolbiecki '15 Dercks, Desai, Kim, Rolbiecki, Tattersall '16

# New analysis implementation

Experimental Cutflow reproduced CheckMATE -----





# Recasting with CM



Show in	CheckMATE	
the color	implementat	
Red dashed	1	
cyan dashed	~	
Gray dashed	1	
Magenta	1	
Blue	~	
Green	×	
Magenta	1	
Red dashed	1	
Green	×	

Compressed spectra searches applied directly ATLAS [1803.02762]
 13 TeV, 36 fb<sup>-1</sup>

ATLAS [1803.02762]
 13 TeV, 36 fb<sup>-1</sup>

ATLAS [1908.08215]
 13 TeV, 139 fb<sup>-1</sup>



### Most relevant in our case

tion



# • $\Delta a_{\mu} = (28.02 \pm 7.37) \times 10^{-10}$

Anticipated future bound  $\Delta a_{\mu}^{fut} = (28.02 \pm 5.2) \times 10^{-10}$ 

$$\Omega_{CDM} h^2 = 0.120 \pm 0.001$$

**Direct detection SI bounds from XENON1T** 

# Parameter Scanning

Chargino co-annihilation region:

100 GeV  $\leq M_1 \leq 1$  TeV,  $M_1 \leq M_2 \leq 1.1M_1$ ,  $1.1M_1 \le \mu \le 10M_1, \quad 5 \le \tan\beta \le 60,$ 100 GeV  $\leq m_{\tilde{l}_L} \leq 1$  TeV,  $m_{\tilde{l}_R} = m_{\tilde{l}_L}$ .

Bino-wino co-annihilation

# Slepton co-annihilation region:

Case-L: SU(2) doublet

100 GeV  $\leq M_1 \leq 1$  TeV,  $M_1 \leq M_2 \leq 10M_1$ ,  $1.1M_1 \le \mu \le 10M_1, \quad 5 \le \tan \beta \le 60,$  $M_1 \text{ GeV} \le m_{\tilde{l}_L} \le 1.2M_1, \quad M_1 \le m_{\tilde{l}_R} \le 10M_1.$ 

Case-R: SU(2) singlet

100 GeV  $\leq M_1 \leq 1$  TeV,  $M_1 \leq M_2 \leq 10M_1$ ,  $1.1M_1 \le \mu \le 10M_1, \quad 5 \le \tan \beta \le 60,$  $M_1 \text{ GeV} \le m_{\tilde{l}_R} \le 1.2 M_1, \quad M_1 \le m_{\tilde{l}_L} \le 10 M_1.$ 

MC, S.Heinemeyer, I.Saha 2006.15157



# Chargino Co-annihilation



Upper and lower bounds from  $(g - 2)_{\mu}$  and LHC searches (for compressed spectrum)



R-sleptons heavy, Considerable BR for  $\tilde{e}_L(\tilde{\mu}_L) \rightarrow \tilde{\chi}_1^{\pm} \nu_e(\nu_\mu)$  — Less no. of signal leptons.

# Possibility of A-pole annihilation







Black contour : simplified application of  $H/A \rightarrow \tau^+ \tau^-$ A-pole annihilation strongly constrained 





# Slepton Co-annihilation: Case-L



The left-sleptons and sneutrinos are close in mass to the LSP





(3I + missing  $E_T$ ) exclusion limit weakens ...



Large BR( $\tilde{\chi}_1^{\pm} \to \tilde{\tau}_1 \nu_{\tau}$ ) and BR( $\tilde{\chi}_2^0 \to \tilde{\tau}_1 \tau$ ), BR( $\tilde{\chi}_2^0 \to \tilde{\nu} \nu$ )

# $\frac{\text{Slepton Co-annihilation: Case-L}}{\text{Current } (g-2)_{\mu} \text{ limit}} \xrightarrow{\text{Anticipated future } (g-2)_{\mu} \text{ limit}}$





# DM with low abundance

# $\Omega_{CDM} h^2 \le 0.122$

2103.XXXXX, WITH SVEN HEINEMEYER AND IPSITA SAHA



# DM with Low abundance

# Wino LSP

100 GeV  $\leq M_2 \leq 1.5$  TeV,  $1.1M_2 \leq M_1 \leq 10M_2$ ,  $1.1M_2 \le \mu \le 10M_2, \quad 5 \le \tan \beta \le 60,$ 100 GeV  $\leq m_{\tilde{l}_L}, m_{\tilde{l}_R} \leq 2$  TeV.

Wino  $SU(2)_L$  triplet

Under-abundant upto ~ 3 TeV

Compressed spectra with  $m_{\tilde{\chi}_1^0} \sim m_{\tilde{\chi}_1^{\pm}}$ 

 $\Omega_{CDM}h^2 \le 0.122$ 

# Higgsino LSP

100 GeV  $\leq \mu \leq 1.2$  TeV,  $1.1\mu \leq M_1 \leq 10\mu$ ,  $1.1\mu \le M_2 \le 10\mu, \quad 5 \le \tan\beta \le 60,$ 100 GeV  $\leq m_{\tilde{l}_L}, m_{\tilde{l}_R} \leq 2$  TeV.

Higgsino  $SU(2)_L$  doublet

Under-abundant upto ~ 1 TeV

Compressed spectra with  $m_{\tilde{\chi}_1^0} \sim m_{\tilde{\chi}_1^\pm} \sim m_{\tilde{\chi}_2^0}$ 

# LHC searches

<u>Compressed spectra searches</u>

Soft leptons : ISR jet required to give boost



### ATLAS 1911.12606

# LHC searches

# • Disappearing track searches



 $\Delta m \sim 100$  MeV

 $\tilde{\chi}_1^{\pm} \to \pi^{\pm} \tilde{\chi}_1^0$ 

Finite lifetime, decay within detector

FIG. 1: Required number of hits in the ATLAS inner tracker for the analyses of Run-1&2 and ours.



![](_page_32_Picture_0.jpeg)

# Current $(g-2)_{\mu}$ limit

![](_page_32_Figure_2.jpeg)

- Compressed spectra searches most important.
- Slepton pair production searches also relevant
- $\Delta m \sim \mathcal{O}(10)$  GeV  $\rightarrow$  Disappearing track searches not sensitive

$$c\tau \simeq 0.7 \text{ cm} \times \left[ \left( \frac{\Delta m_+}{340 \text{ MeV}} \right)^3 \sqrt{1 - \frac{m_+^2}{\Delta m^2}} \right]$$

![](_page_32_Figure_7.jpeg)

![](_page_32_Figure_8.jpeg)

# Higgsino LSP

# Current $(g-2)_{\mu}$ limit

![](_page_33_Figure_2.jpeg)

Future 
$$(g-2)_{\mu}$$
 limit

![](_page_33_Figure_4.jpeg)

![](_page_34_Figure_0.jpeg)

800

 Slepton pair production searches important

• 
$$(g-2)_{\mu}$$
 Dominated by  $\tilde{\chi}_1^{\pm} - \tilde{\nu}$  loop

- Higher slepton masses conflict with DM DD
- Substantial  $\tilde{e}_L(\tilde{\mu}_L) \rightarrow \tilde{\chi}_1^{\pm} \nu_e(\nu_{\mu})$
- 2 lepton + missing  $E_T$  bound weakens

# Higgsino LSP direct detection

![](_page_35_Figure_1.jpeg)

$$|\mathbf{x}| = c_{h\tilde{\chi}_{1}^{0}\tilde{\chi}_{1}^{0}} \simeq -\frac{1}{2}(1+\sin 2\beta) \left(\tan^{2}\theta_{w}\frac{M_{W}}{M_{1}-\mu} + \frac{M_{W}}{M_{2}}\right)$$

![](_page_35_Picture_3.jpeg)

# Wino LSP

![](_page_36_Figure_1.jpeg)

### Highly degenerate $\tilde{\chi}_1^{\pm}$ and $\tilde{\chi}_1^0$

# Tree level splitting from $\tilde{h}$ mixing

$$\simeq \frac{M_W^4 (\sin 2\beta)^2 \tan^2 \theta_w}{(M_1 - M_2)\mu^2}$$

EW 1 loop correction  $\Delta m \sim 170 \text{ MeV}$ 

Ibe, Matsumoto, Sato '13

![](_page_36_Picture_7.jpeg)

# Wino LSP

![](_page_37_Figure_1.jpeg)

High  $\Delta m$  restricted by DD Low  $\Delta m$  restricted by LHC

• Tree level splitting from  $\tilde{h}$  mixing

$$\simeq \frac{M_W^4 (\sin 2\beta)^2 \tan^2 \theta_w}{(M_1 - M_2)\mu^2}$$

• Coupling for DD  

$$c_{h\tilde{\chi}_1^0\tilde{\chi}_1^0} \simeq \frac{M_W}{M_2^2 - \mu^2} (M_2 + \mu \sin 2\beta),$$

Ibe, Matsumoto, Sato '13

![](_page_37_Picture_7.jpeg)

# Wino LSP lifetime

# Current $(g-2)_{\mu}$ limit

 $\Gamma(\tilde{\chi}^{\pm})$ 

![](_page_38_Figure_2.jpeg)

$$\rightarrow \tilde{\chi}^0 \pi^{\pm}) = \Gamma(\pi^{\pm} \to \mu^{\pm} \nu_{\mu}) \times \frac{16\delta m^3}{m_{\pi} m_{\mu}^2} \left(1 - \frac{m_{\pi}^2}{\delta m^2}\right)^{1/2} \left(1 - \frac{m_{\pi}^2}{m_{\pi}^2}\right)^{1/2} \left(1$$

Disappearing track searches most important.

![](_page_38_Figure_5.jpeg)

# Wino LSP

![](_page_39_Figure_1.jpeg)

![](_page_39_Figure_2.jpeg)

# Wino LSP : Direct detection

Current  $(g-2)_{\mu}$  limit

![](_page_40_Figure_2.jpeg)

# • DD coupling $c_{h\tilde{\chi}_1^0\tilde{\chi}_1^0} \simeq \frac{M_W}{M_2^2 - \mu^2} (M_2 + \mu \sin 2\beta),$

 All allowed points to be checked by XENONnT

## Results in the $m_{\tilde{\chi}_1^0} - m_{\tilde{l}_1}$ plane Current $(g - 2)_{\mu}$ limit $1600_{1}$ 1400 1200 $m_{\widetilde{\mu}_1^\pm}$ (GeV) 1000 800 600 WINO 400 $(g-2)_{\mu} + \Omega h^2$ $(g-2)_{\mu} + \Omega h^2 + DD$ 200 $(g-2)_{\mu} + \Omega h^2 + DD + LHC$ 800 500 600 700 200 300 400 100 $m_{\widetilde{\chi}_1^0}$ (GeV)

Future 
$$(g - 2)_{\mu}$$
 limit

![](_page_41_Figure_3.jpeg)

# A-pole annihilation

![](_page_42_Figure_1.jpeg)

Black contour:  $H/A \to \tau^+ \tau^-$ ,  $M_h^{125}(\tilde{\chi})$  Benchmark scenario

![](_page_42_Figure_3.jpeg)

# Future prospects

![](_page_43_Figure_1.jpeg)

# Conclusions

- collider limits.
- DM and muon (g-2) constraints put effective upper limit on EW SUSY masses.
- LHC limits restrict the mass ranges from below.
- Proper recasting of ATLAS/CMS analyses important!
- Future collider searches and DD experiments have the potential to be conclusive.
- New experimental results for  $(g 2)_{\mu}$  from Fermilab, J-PARC .... STAY TUNED!!!

• It is possible to constrain the EW MSSM with the help of indirect constraints along with the direct

![](_page_44_Picture_13.jpeg)

![](_page_45_Picture_1.jpeg)

![](_page_46_Picture_0.jpeg)

# MSSM Superpotential

# Soft Breaking Terms

$$\mathscr{L}_{\text{soft}}^{\text{MSSM}} = -\frac{1}{2} \left( M_3 \tilde{g} \tilde{g} + M_2 \tilde{W} \tilde{W} + M_1 \tilde{B} \tilde{B} + c \cdot c \right)$$
$$- \left( \tilde{u} \mathbf{a}_{\mathbf{u}} \tilde{Q} H_u - \tilde{d} \mathbf{a}_{\mathbf{d}} \tilde{Q} H_d - \tilde{e} \mathbf{a}_{\mathbf{e}} \tilde{L} H_d + c \cdot c \right)$$
$$- \tilde{Q}^{\dagger} \mathbf{m}_{\mathbf{Q}}^2 \tilde{Q} - \tilde{L}^{\dagger} \mathbf{m}_{\mathbf{L}}^2 \tilde{L} - \tilde{u} \mathbf{m}_{\mathbf{u}}^2 \tilde{u}^{\dagger} - \tilde{d} \mathbf{m}_{\mathbf{d}}^2 \tilde{d}^{\dagger} - \tilde{e} \mathbf{m}_{\mathbf{e}}^2 \tilde{e}^{\dagger}$$
$$- m_{H_u}^2 H_u^* H_u - m_{H_d}^2 H_d^* H_d - \left( b H_u H_d + c \cdot c \right)$$

![](_page_47_Picture_4.jpeg)

# $W_{\rm MSSM} = \bar{u}Y_uQH_u - \bar{d}Y_dQH_d - \bar{e}Y_eLH_d + \mu H_uH_d$

### $(-2)_{\mu}$

- Large discrepancy from the SM (more than  $3\sigma$ ):  $a_{\mu}^{exp} - a_{\mu}^{SM} = (28.02 \pm 7.37) \times 10^{-10}.$
- Important probe for new physics.  $\frac{\delta a_l}{a_l} \sim \frac{m_l^2}{\Lambda^2}$ .
- hadronic light by light scattering.
- QED : complete calculation up to 5 loops. EW : two loops. Aoyama, Hayakawa, Kinoshita, Nio '17, Ishikawa, Nakazawa, Yasu '18, Heinemeyer, Stökinger, Weiglein '04
- Uncertainty dominated by non-perturbative, hadronic sector.

![](_page_48_Figure_6.jpeg)

Keshavarzi, Nomura, Teubner '19

• SM contributions : QED, weak, hadronic vacuum polarization,

![](_page_48_Figure_13.jpeg)

![](_page_49_Figure_0.jpeg)

given by the LEP2 constraints [30]-[33].

Figure 6: The lifetime of charged wino evaluated by using  $\delta m$  at the one-loop (green band) and two-loop (red band). We neglected the next-to-leading order corrections to the lifetime of the charged wino estimated in terms of the pion decay rate, which is expected to be a few percent correction. The black chain line is the upper limit on the lifetime for a given chargino mass by the ATLAS collaboration at  $95\,\%\,\mathrm{CL}$  $(\sqrt{s} = 7 \text{ TeV}, \mathcal{L} = 4.7 \text{ fb}^{-1})$  [28]. The blue line shows the constraints which are

# Highest mass points

Current  $(g-2)_{\mu}$  limit

Coannihilation	$\tilde{\chi}_1^{\pm}$	$\tilde{l}^{\pm}$ (Case-L)	$\tilde{l}^{\pm}$ (Case-R)
$m_{ ilde{\chi}_1^0}$	570	533	518
$m_{ ilde{\chi}_2^0}$	605	816	685
$m_{ ilde{\chi}_3^0}$	1087	1370	1098
$m_{\tilde{\chi}_1^{\pm}}$	605	816	685
$m_{\tilde{e}_1,\tilde{\mu}_1}$	680	549	696
$m_{ ilde{e}_2, ilde{\mu}_2}$	680	1279	592
$m_{ ilde{ au}_1}$	582	534	747
$m_{ ilde{ au}_2}$	765	1286	526
$m_{ ilde{ u}}$	675	544	692

Points satisfying  $(g - 2)_{\mu}$ , DM and LHC constraints, masses in GeV.

# Anticipated future $(g - 2)_{\mu}$ limit

Coannihilation	$\tilde{\chi}_1^{\pm}$	$\tilde{l}^{\pm}$ (Case-L)	$\tilde{l}^{\pm}$ (Case-R)
$m_{ ilde{\chi}_1^0}$	423	499	402
$m_{ ilde{\chi}_2^0}$	464	535	448
$m_{ ilde{\chi}_3^0}$	1032	1019	830
$m_{\tilde{\chi}_1^{\pm}}$	464	535	448
$m_{ ilde{e}_1, ilde{\mu}_1}$	542	511	795
$m_{ ilde{e}_2, ilde{\mu}_2}$	541	2349	428
$m_{ ilde{ au}_1}$	437	509	807
$m_{ ilde{ au}_2}$	629	2350	406
$m_{ ilde{ u}}$	536	505	792

![](_page_50_Picture_7.jpeg)